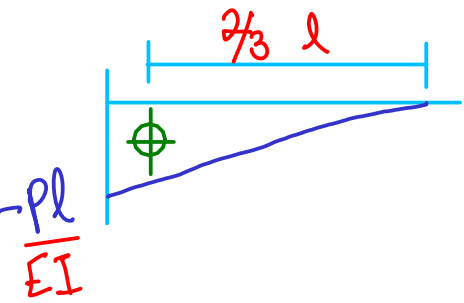


Calcule la pendiente teta B y la deflexión en B en el extremo de la viga en voladizo. EI es constante.

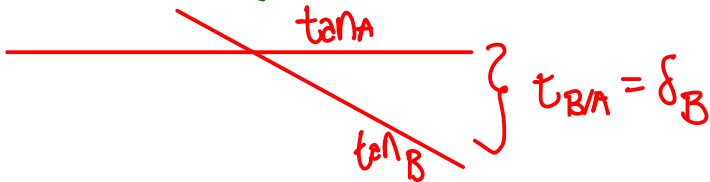
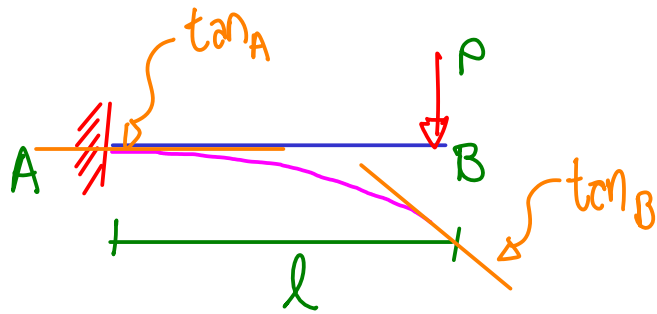


$$\Delta \theta_{AB} = \int_A^B \frac{M}{EI} dx$$

$$\theta_A + \Delta \theta_{AB} = \theta_B$$

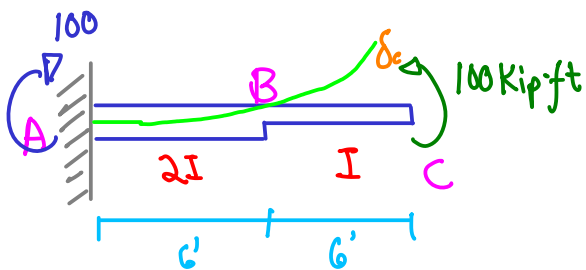
$$\Delta \theta_{AB} = \frac{1}{2} l \left(\frac{-Pl}{EI} \right) = \frac{-Pl^2}{2EI}$$

$$\theta_B = 0 + \frac{-Pl^2}{2EI} = \frac{-Pl^2}{2EI} //$$



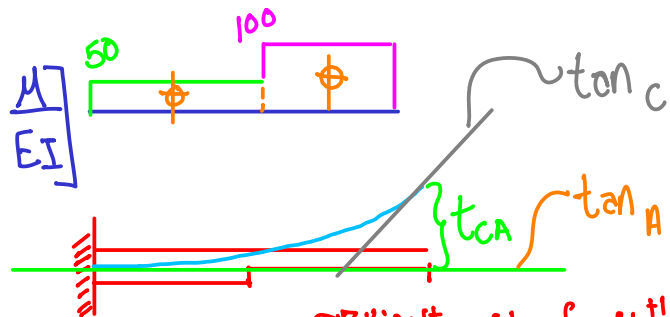
$$t_{B/A} = \int_A^B \frac{Mx}{EI} dx$$

$$t_{B/A} = \frac{1}{2} l \left(\frac{-Pl}{EI} \right) \left(\frac{2}{3} l \right) = \frac{-Pl^3}{3EI}$$



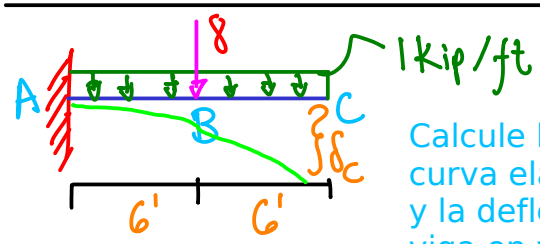
Calcule la deflexión del punto C en el extremo de la viga en voladizo si $E = 29,000$ ksi; $l_{AB} = 2l$; $l_{BC} = l$; $E =$ constante; $I = 400$ in⁴.



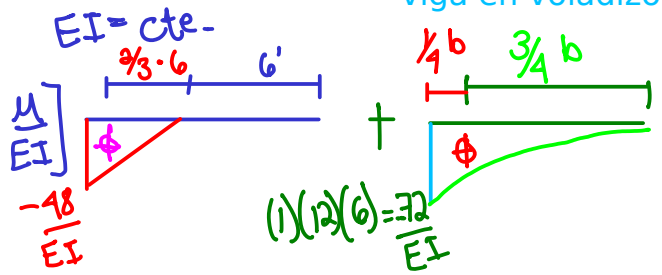


$$t_{CA} = \int_A^C \frac{Mx}{EI} dx = EI \delta_C = (50)(6)(3+6) + (100)(6)(3) = 4500$$

$$\delta_C = \frac{4500}{EI} = \frac{4500 \text{ Kip} \cdot \text{ft}^3}{(29,000 \text{ ksi})(400 \text{ in}^4)} \left(12 \cdot 12 \cdot 12 \frac{\text{in}^3}{\text{ft}^3} \right) = 0.67 \text{ in}$$



Calcule la pendiente de la curva elástica en B y en C; y la deflexión en C para la viga en voladizo.



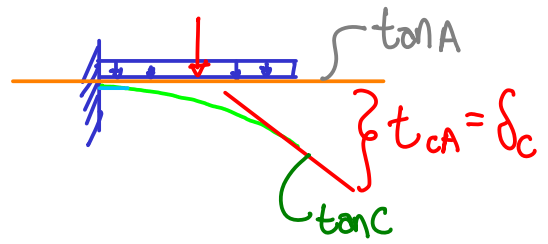
$$\theta_C = \theta_A + \Delta\theta_{AC} = 0 + \int_A^C \frac{M}{EI} dx$$

$$\theta_C = \frac{1}{2}(6) \left(\frac{-48}{EI} \right) + \frac{1}{3}(12) \left(\frac{-72}{EI} \right)$$

$$\theta_C = \frac{-144}{EI} - \frac{288}{EI} = \frac{-432}{EI} \text{ rad}$$

$$\delta_C = t_{CA} = \int_A^C \frac{Mx}{EI} dx$$

$$\delta_C = \frac{1}{2}(6) \left(\frac{-48}{EI} \right) \left(6 + \frac{2}{3} \cdot 6 \right) + \frac{1}{3}(12) \left(\frac{-72}{EI} \right) \left(\frac{3}{4} \cdot 12 \right)$$



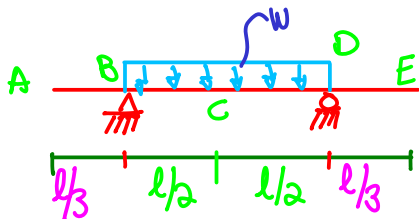
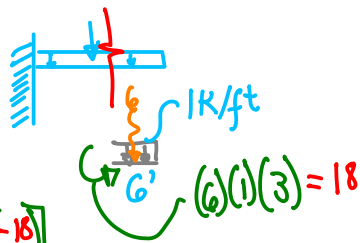
$$\delta_C = \frac{-144}{EI} (10) - \frac{288}{EI} (9) = \frac{-1440 - 2592}{EI} = \frac{-4032}{EI}$$

Pendiente o rotación en B

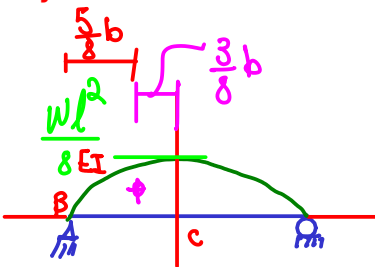
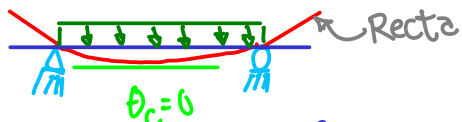
$$\theta_B = \theta_A + \Delta\theta_{AB} = 0 + \int_A^B \frac{M}{EI} dx$$

$$= \frac{1}{2}(6) \left(\frac{-18}{EI} \right) + \left[\frac{1}{3}(12) \left(\frac{-72}{EI} \right) - \frac{1}{3}(6) \left(\frac{-18}{EI} \right) \right]$$

$$= \frac{-144}{EI} + \frac{-252}{EI} = \frac{-396}{EI} \text{ rad.}$$

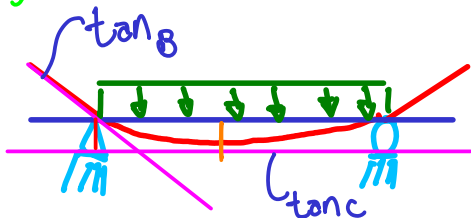


Para la viga, calcule la pendiente en B, y las deflexiones en el punto A y el centro del claro.



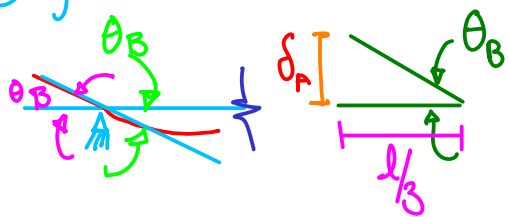
$$\theta_B = \theta_C + \Delta\theta_{CB} = 0 + \int_B^C \frac{M}{EI} dx = \frac{1}{3} \left(\frac{l}{7} \right) \left(\frac{wl^2}{8EI} \right) = \frac{wl^3}{24EI}$$

Deflexión en C



$$t_{BC} = \delta_c = \frac{2}{3} \left(\frac{l}{7} \right) \left(\frac{wl^2}{8EI} \right) \left(\frac{5}{8} \cdot \frac{l}{2} \right) = \frac{5wl^4}{384EI}$$

Deflexión en A



$$\delta_A = \theta_B \left(\frac{l}{3} \right) = \frac{wl^3}{24EI} \left(\frac{l}{3} \right) = \frac{wl^4}{72EI}$$