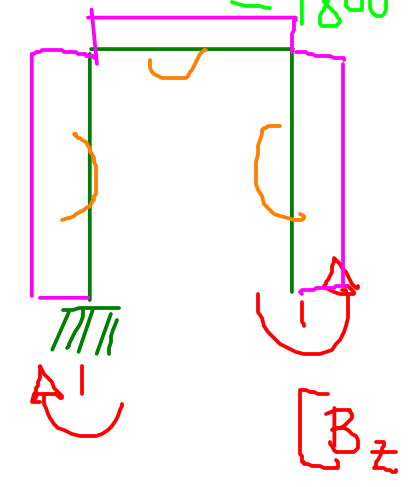
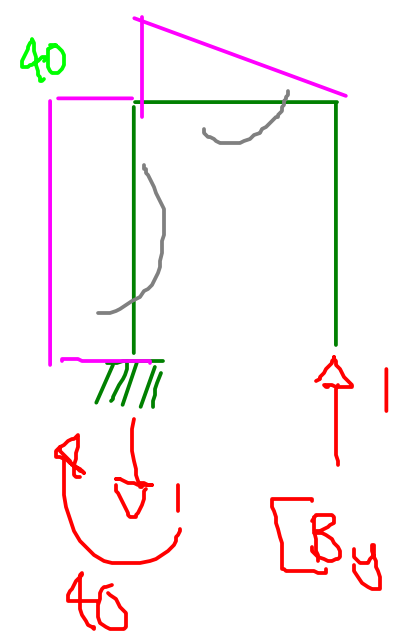
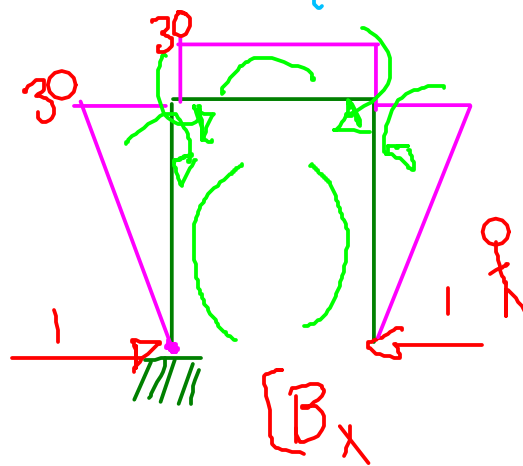


$$M = 20(30) + 1.5(40)(20) = 1800$$



Tramo	Origen	Limites	M_p	M_{Q_x}	M_{Q_y}	M_{Q_z}
AC	A	0-30	$-1800 + 20x$	$-x$	40	
CD	D	0-40	$-1.5x(\frac{x}{2})$	-30	x	
DB	B	0-30	0	x	0	-

$$\Delta_{x0} = \int_0^{30} \frac{(-1800 + 20x)(-x)}{EI} dx + \int_0^{40} \frac{-0.75x^2(-30)}{2EI} dx + \int_0^{30} \frac{(0)(x)}{EI} dx$$

$$\Delta y_0 = \int_0^{30} \frac{(-1800 + 20x)(40) dx}{EI} + \int_0^{40} \frac{-0.75x^2(x) dx}{2EI}$$

$$+ \int_0^{30} \frac{(0)(0) dx}{EI}$$

$$\Theta_{z_0} = \int_0^{30} \frac{(-1800 + 20x)(1) dx}{EI} + \int_0^{40} \frac{(-0.75x^2)(1) dx}{2EI}$$

$$+ \int_0^{30} \frac{(0)(-1) dx}{EI}$$

$$\delta_{x,x} = \int_0^{30} \frac{(-x)(-x) dx}{EI} + \int_0^{40} \frac{(-30)(-30) dx}{2EI} + \int_0^{30} \frac{(x)(x) dx}{EI}$$

$$\delta_{y,y} = \int_0^{30} \frac{(40)(40) dx}{EI} + \int_0^{40} \frac{(x)(x) dx}{2EI} + \int_0^{30} \frac{(0)(0) dx}{EI}$$

$$\delta_{z,z} = \int_0^{30} \frac{(1)(1) dx}{EI} + \int_0^{40} \frac{(1)(1) dx}{2EI} + \int_0^{30} \frac{(-1)(-1) dx}{EI}$$

$$\delta_{x,y} = \delta_{y,x} = \int_0^{30} \frac{(-x)(40) dx}{EI} + \int_0^{40} \frac{-30(x) dx}{2EI} + \int_0^{30} \frac{x(0) dx}{EI}$$

$$\delta_{x,z} = \delta_{z,x} = \int_0^{30} \frac{(-x)(1) dx}{EI} + \int_0^{40} \frac{-30(1) dx}{2EI} + \int_0^{30} \frac{x(-1) dx}{EI}$$

$$\delta_{y,z} = \delta_{z,y} = \int_0^{30} \frac{(40)(1) dx}{EI} + \int_0^{40} \frac{(x)(1) dx}{2EI} + \int_0^{30} \frac{(0)(-1) dx}{EI}$$

$$\Delta_{x0} = \int_0^{30} (-1800 + 20 \cdot x) \cdot (-x) dx + \int_0^{40} \frac{-0.75 \cdot x^2 \cdot (-30)}{2} dx + \int_0^{30} 0 \cdot x dx = 8.7 \cdot 10^5$$

$$\Delta_{y0} = \int_0^{30} (-1800 + 20 \cdot x) \cdot (40) dx + \int_0^{40} \frac{-0.75 \cdot x^2 \cdot (x)}{2} dx + \int_0^{30} 0 \cdot 0 dx = -2.04 \cdot 10^6$$

$$\theta_{z0} = \int_0^{30} (-1800 + 20 \cdot x) \cdot (1) dx + \int_0^{40} \frac{-0.75 \cdot x^2 \cdot (1)}{2} dx + \int_0^{30} 0 \cdot (-1) dx = -53000$$

$$\delta_{xx} = \int_0^{30} (-x)^2 dx + \int_0^{40} \frac{(-30)^2}{2} dx + \int_0^{30} x^2 dx = 36000$$

$$\delta_{yy} = \int_0^{30} (40)^2 dx + \int_0^{40} \frac{(x)^2}{2} dx + \int_0^{30} 0^2 dx = 58666.6667$$

$$\delta_{zz} = \int_0^{30} (1)^2 dx + \int_0^{40} \frac{(1)^2}{2} dx + \int_0^{30} (-1)^2 dx = 80$$

$$\delta_{xy} = \int_0^{30} -x \cdot 40 dx + \int_0^{40} \frac{-30 \cdot x}{2} dx + \int_0^{30} x \cdot 0 dx = -30000 \quad \delta_{yx} = \delta_{xy}$$

$$\delta_{xz} = \int_0^{30} -x \cdot 1 dx + \int_0^{40} \frac{-30 \cdot 1}{2} dx + \int_0^{30} x \cdot (-1) dx = -1500 \quad \delta_{zx} = \delta_{xz}$$

$$\delta_{yz} = \int_0^{30} 40 \cdot 1 dx + \int_0^{40} \frac{x \cdot 1}{2} dx + \int_0^{30} 0 \cdot (-1) dx = 1600 \quad \delta_{zy} = \delta_{yz}$$

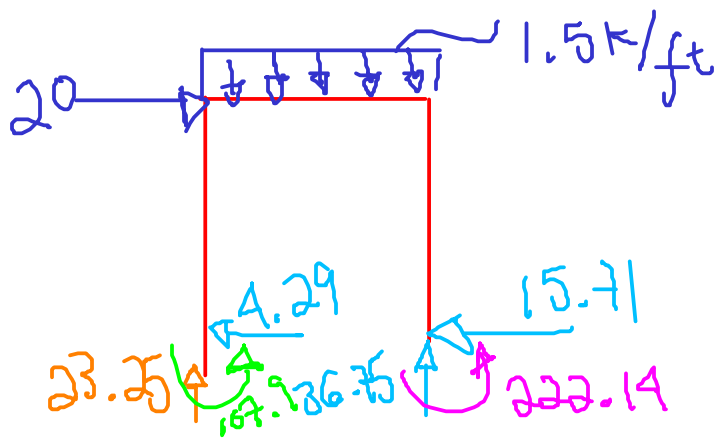
$$\Delta_{x0} + \delta_{xx} B_x + \delta_{xy} B_y + \delta_{xz} B_z = 0$$

$$\Delta_{y0} + \delta_{yx} B_x + \delta_{yy} B_y + \delta_{yz} B_z = 0$$

$$\theta_{z0} + \delta_{zx} B_x + \delta_{zy} B_y + \delta_{zz} B_z = 0$$

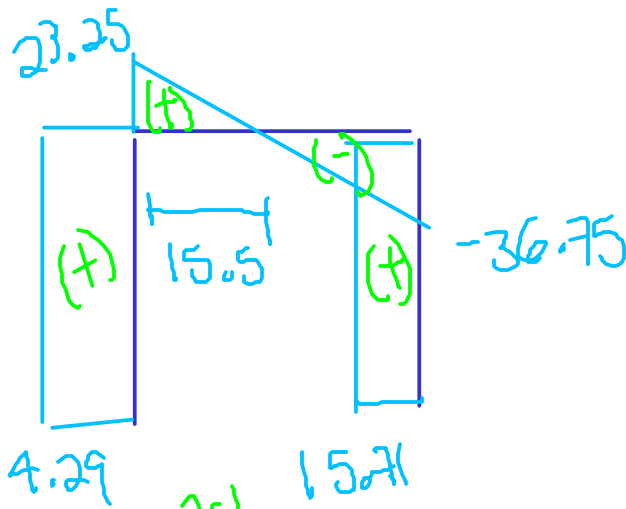
$$\begin{bmatrix} \delta_{xx} & \delta_{xy} & \delta_{xz} \\ \delta_{yx} & \delta_{yy} & \delta_{yz} \\ \delta_{zx} & \delta_{zy} & \delta_{zz} \end{bmatrix}^{-1} \cdot \begin{bmatrix} \Delta_{x0} \\ \Delta_{y0} \\ \theta_{z0} \end{bmatrix} = \begin{bmatrix} 15.7143 \\ 36.75 \\ 222.1429 \end{bmatrix} \begin{matrix} B_x \\ B_y \\ B_z \end{matrix}$$

$$\begin{aligned} \sum M_A &= 20(30) + 1.5(40)(20) \\ &= 36.75(40) - 222.14 + M_A = 0 \\ M_A &= -107.9 \end{aligned}$$



$$\begin{aligned} (1.5)(40) &= 60 \\ 60 - 36.75 &= 23.25 \\ 20 - 15.71 &= 4.29 \end{aligned}$$

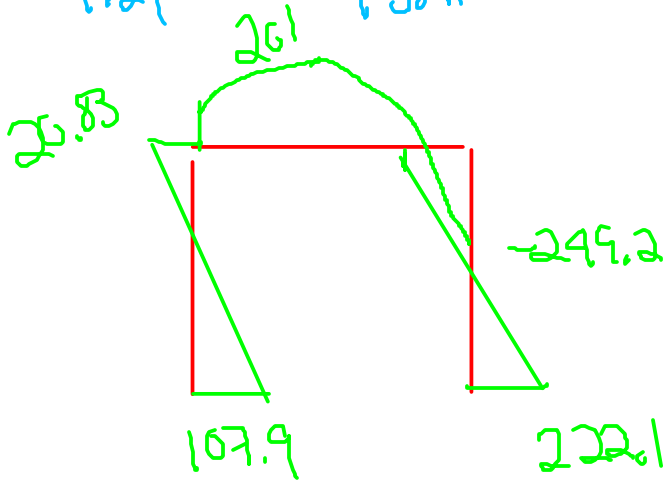
V



$$23.25 - 1.5x = 0$$

$$x = 15.5$$

M



$$-107.9 + 4.29(30) = 20.83$$

$$20.83 + \frac{1}{2}(15.5)(23.25) = 201$$

$$201 - \frac{1}{2}(40 - 15.5)(36.75) = -249.2$$

$$-249.2 + 15.71(30) = 222.1$$