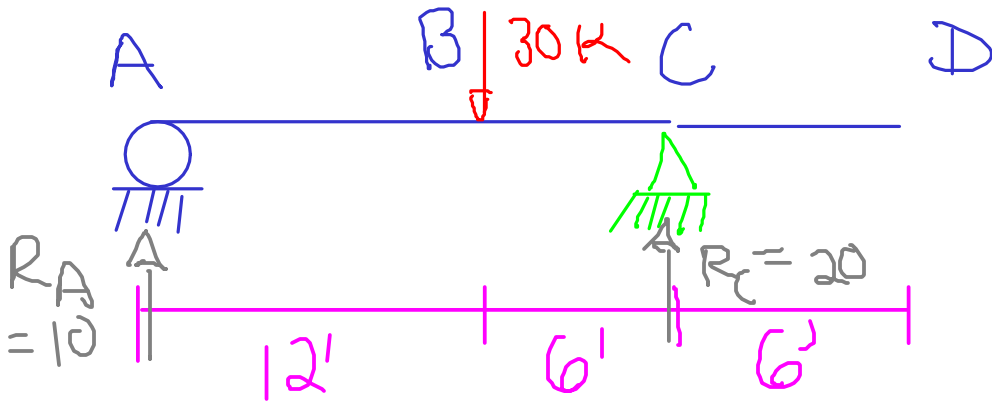
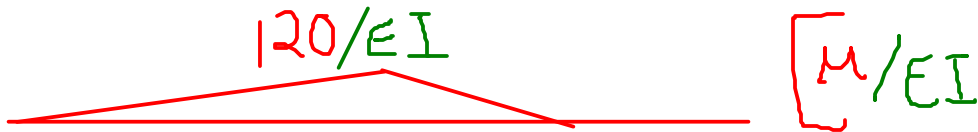
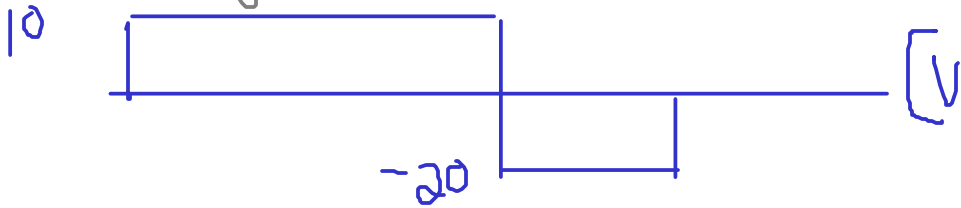


Obtener la deflexión máxima de A a C, y la deflexión en D.

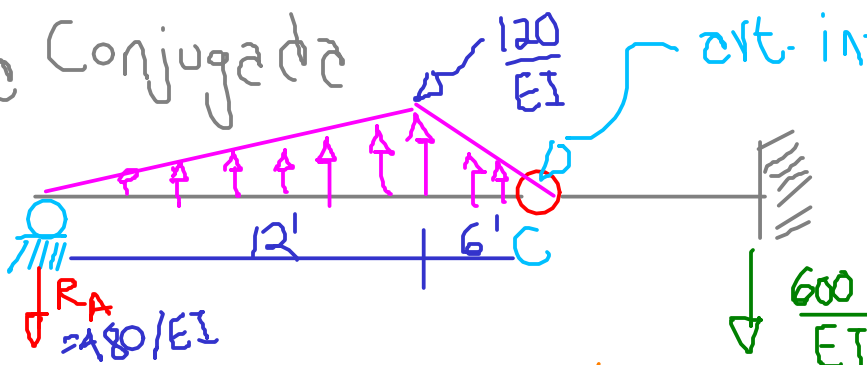


$$\sum M_C = R_A(18) - 30(6) = 0 \rightarrow R_A = 10 \text{ k} \uparrow$$

$$\sum F_y = 10 - 30 + R_C = 0 \rightarrow R_C = 20 \text{ k} \uparrow$$



Viga Conjugada



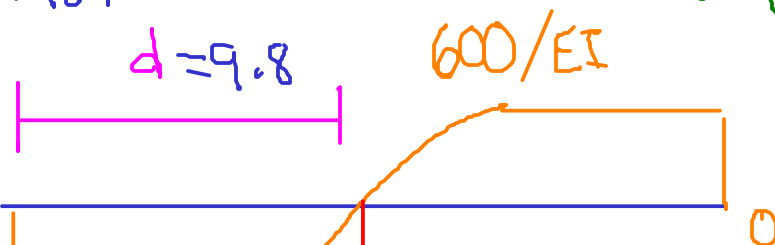
art. interno (Lado Izquierdo)

$$\sum M_C = R_A(18) -$$

$$\frac{1}{2}(12)\left(\frac{120}{EI}\right)\left(6 + \frac{1}{3} \cdot 12\right) - \frac{1}{2}(6)\left(\frac{120}{EI}\right)\left(\frac{2}{3} \cdot 6\right)$$

$$= 0 \rightarrow R_A = 480/EI$$

V_C
 θ_{VR}
 $-\frac{480}{EI}$



$$\frac{x}{12} = \frac{y}{\frac{120}{EI}}$$

$$y = \frac{120}{EI} \cdot \frac{x}{12} = \frac{10x}{EI}$$

$$\sum F_y = -\frac{480}{EI} + \frac{1}{2}(12)\left(\frac{120}{EI}\right) + \frac{1}{2}(6)\left(\frac{120}{EI}\right) + R_D = 0$$

$$R_D = -600/EI$$

$$\frac{480}{EI} = \frac{1}{2} \times \left(\frac{10x}{EI} \right)$$

$$480 = 5x^2$$

$$96 = x^2$$

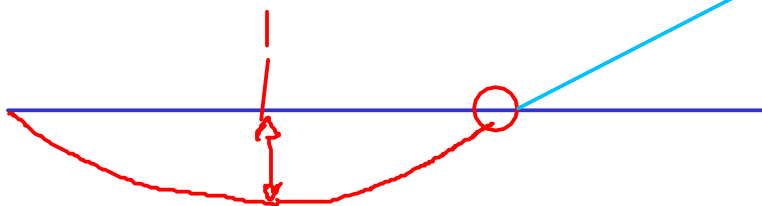
$$\sqrt{96} = x$$

$$x = 9.8$$

$$M_D = \frac{3600}{EI} = \int_D \frac{600}{EI} (6') = \frac{3600}{EI}$$

$$\frac{2}{3} (9.8) \left(\frac{480}{EI} \right) = \frac{3136}{EI}$$

M_{VC}
 δ_{VR}



$$\delta_{AC} = M_{9.8m} = \frac{-3136}{EI}$$

$$15(9) = 135$$

\curvearrowright

15 ↑



15K ↓

B

q ↓

V ↓

15
0

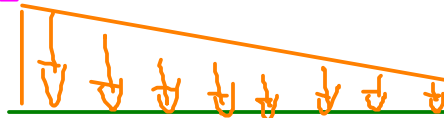
(+)

M ↓

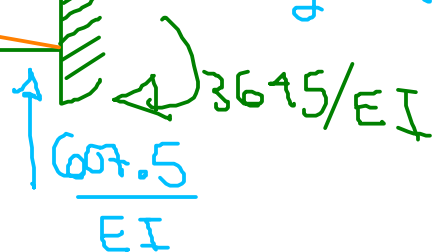


$\frac{-135}{EI}$

$\frac{135}{EI}$



$$R_B = \frac{1}{2} (9) \left(\frac{135}{EI} \right) = \frac{607.5}{EI}$$

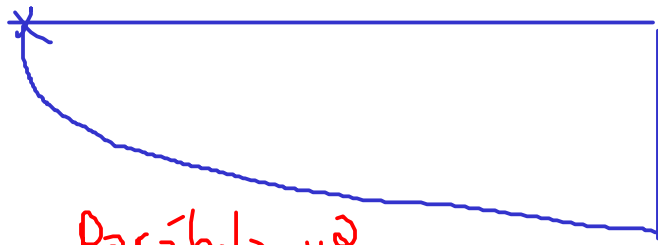


$\delta_B = ?$

$\theta_B = ?$

$$M_B = \frac{1}{2} (9) \left(\frac{135}{EI} \right) \left(\frac{2 \cdot 9}{3} \right) = \frac{3645}{EI}$$

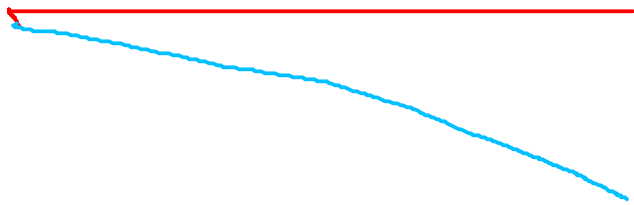
V_{VC}
 θ_{VR}



Parábola x^2

$$-\frac{607.5}{EI} = \theta_B$$

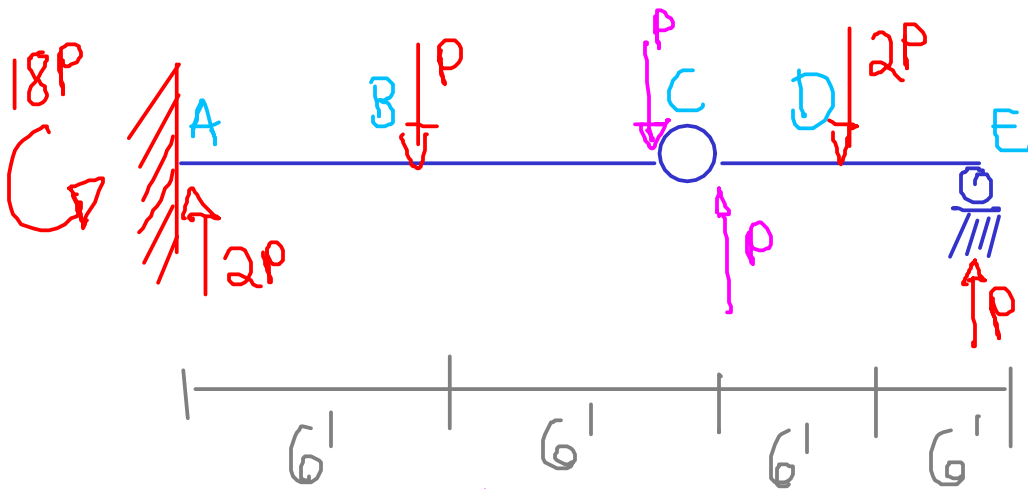
M_{VC}
 δ_{VR}



Parábola x^3

$$\frac{2bh}{3} = \frac{2}{3} (9) \left(\frac{607.5}{EI} \right)$$

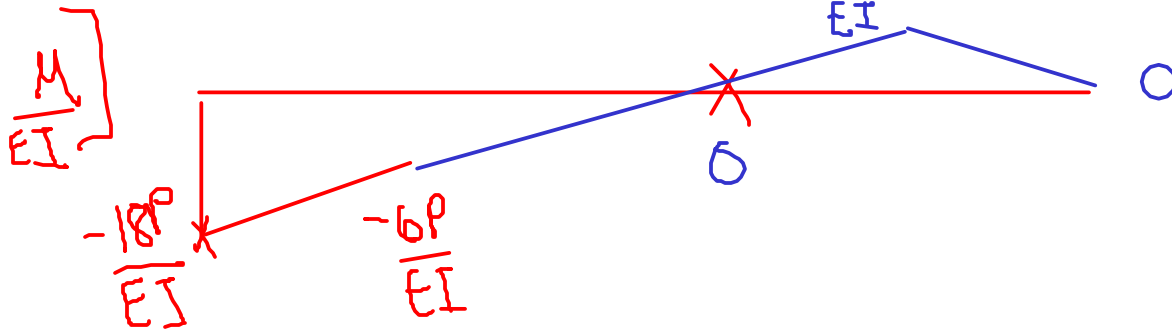
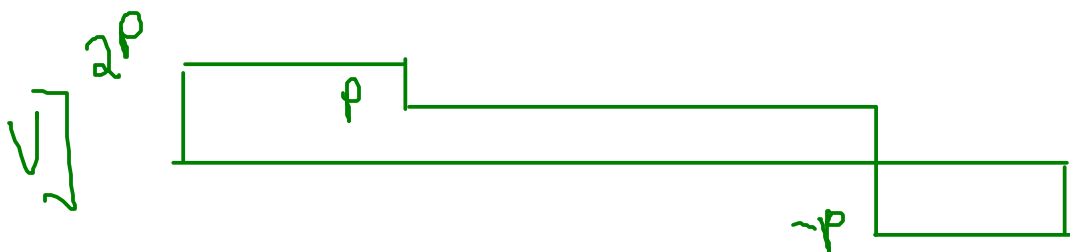
$$-\frac{3645}{EI} = \delta_B$$



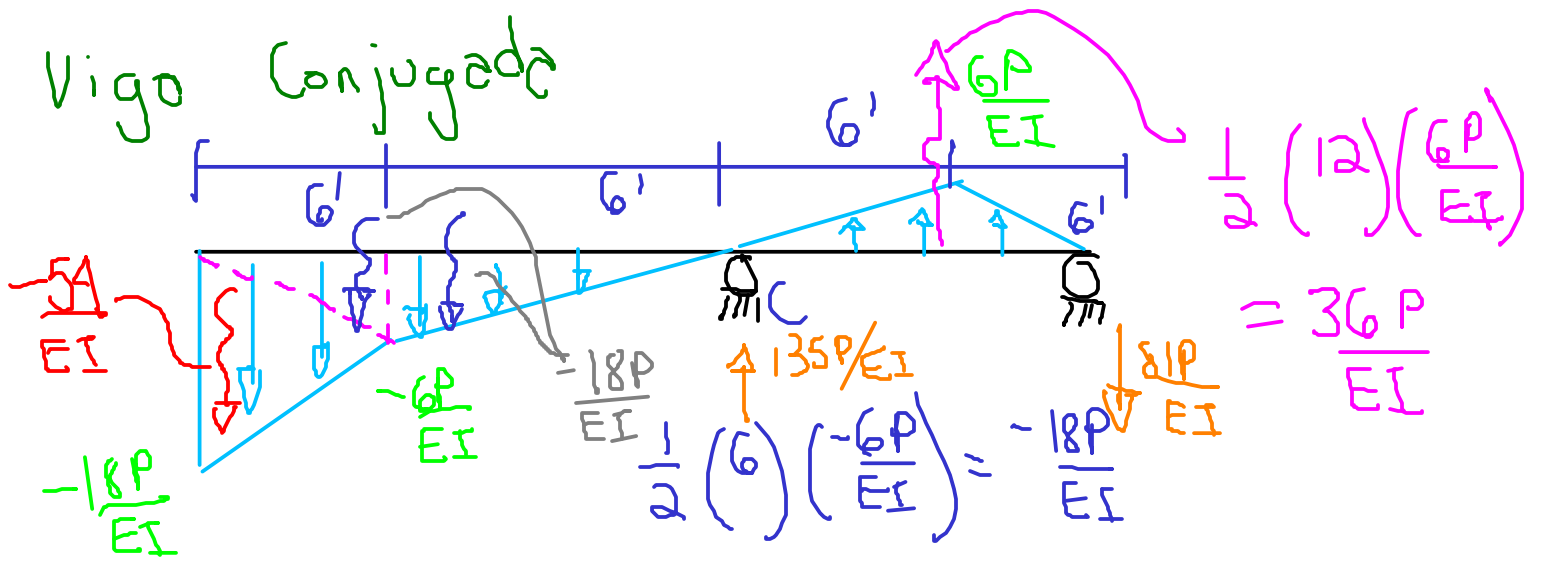
Deflexión Máxima de la Viga

$$M_A = P(6) + P(12) = 0$$

$$M_D = 18P$$



Vigo Conjugada



$$\frac{1}{2}(6)\left(\frac{-18P}{EI}\right) = \frac{-54P}{EI}$$

$$\sum M_C = 0 = \frac{36P}{EI}(6) + \frac{18P}{EI}\left(\frac{2}{3} \cdot 6\right) + \frac{18P}{EI}\left(6 + \frac{1}{3} \cdot 6\right)$$

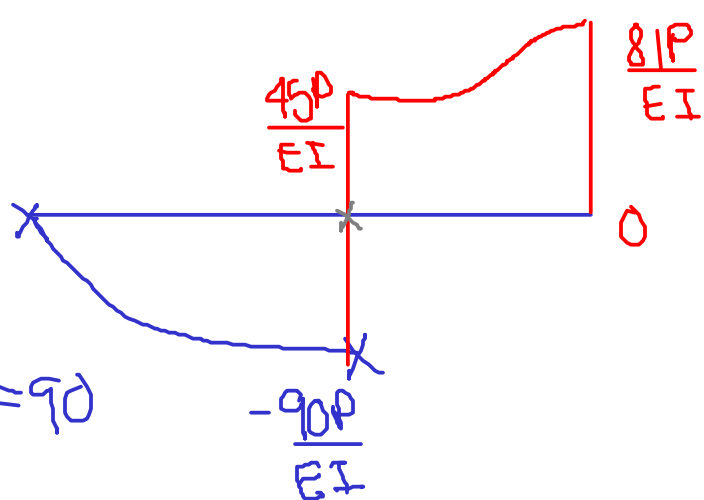
$$+ \frac{54P}{EI}\left(6 + \frac{2}{3} \cdot 6\right) - R_E(12) = 0 \rightarrow R_E = \frac{81P}{EI} \downarrow$$

$$\sum F_y = 0 = \frac{P}{EI}(-54 - 18 - 18 + 36 - 81 + R_C) = 0$$

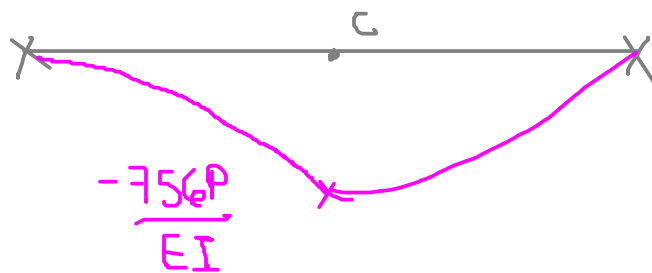
$$R_C = \frac{135P}{EI}$$

$$V_{VC} = \theta_{VR}$$

$$18 + 18 + 54 = 90$$

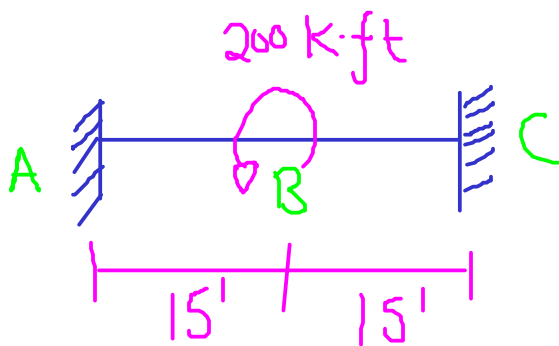
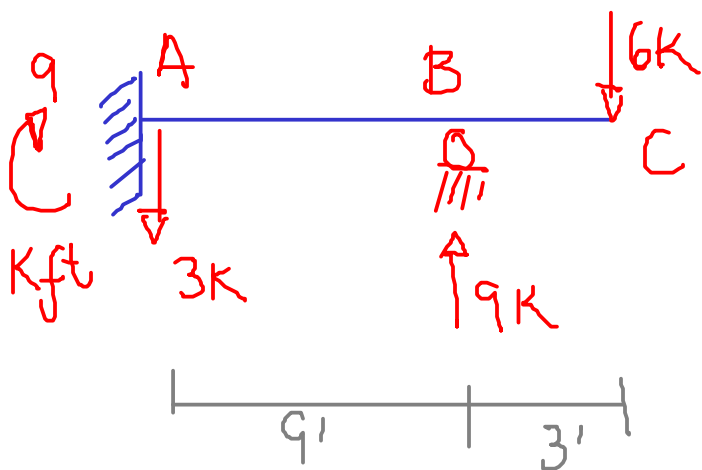


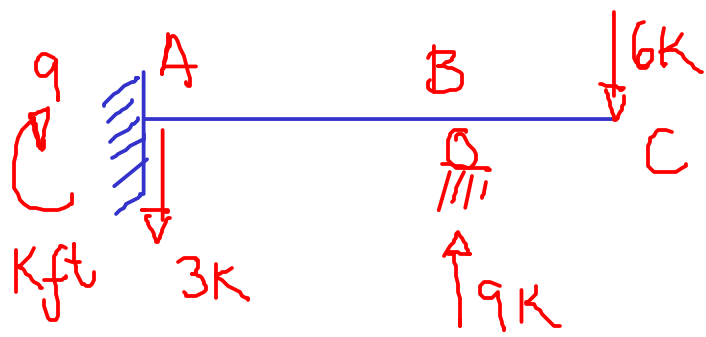
$$M_{VC} = \delta_{VR}$$



$$\sum M_C = \frac{P}{EI} \left[54 \left(6 + \frac{2}{3} \cdot 6 \right) + 18 \left(6 + \frac{1}{3} \cdot 6 \right) + 18 \left(\frac{2}{3} \cdot 6 \right) \right] = \frac{756 P}{EI}$$

$$\delta_{MAX} = -\frac{756 P}{EI}$$

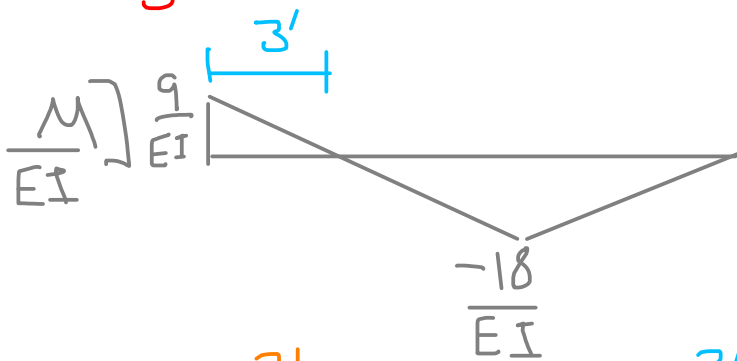
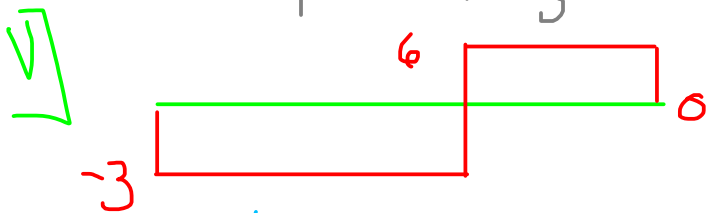




$$\delta_c = ?$$

$\delta_{\text{máx}}$ entre A y B.

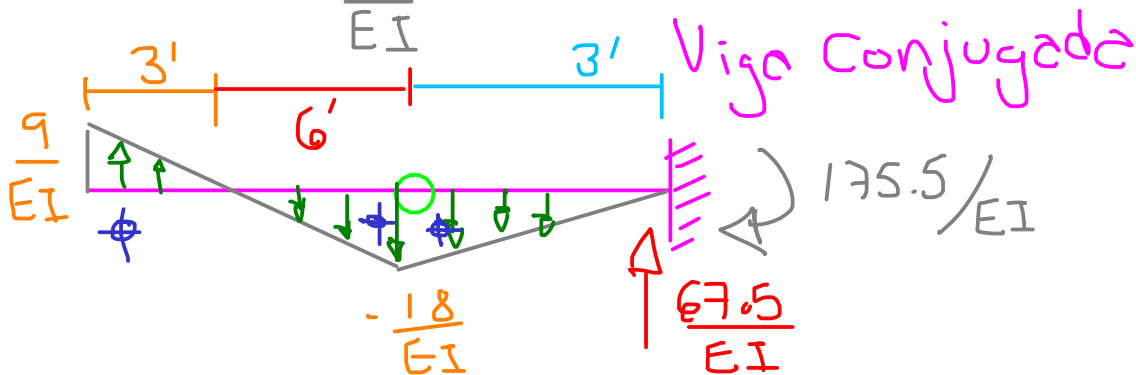
$$EI = \text{cte.}$$



$$9 - (3 \times 9) = -18$$

$$-18 + 6(3) = 0$$

$$9 - 3x = 0 \rightarrow x = 3$$

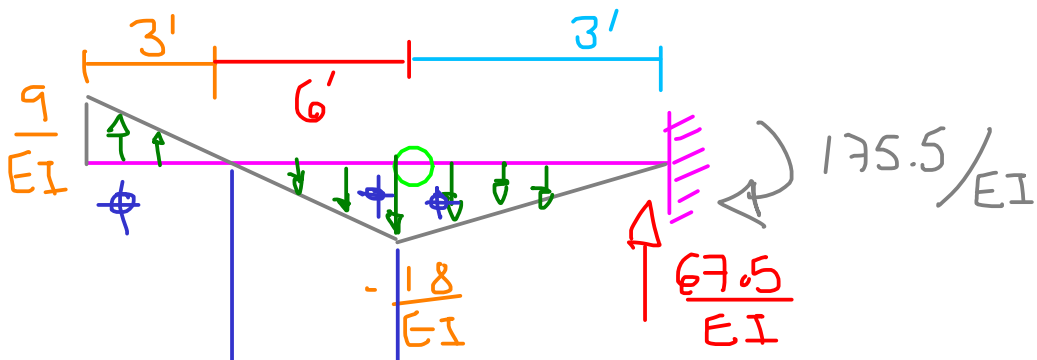


$$\sum F_y = \left(\frac{1}{2}\right)(3')\left(\frac{9}{EI}\right) + \frac{1}{2}(6')\left(\frac{-18}{EI}\right) + \frac{1}{2}(3')\left(\frac{-18}{EI}\right) + R_c = 0$$

$$R_c = 67.5/EI \uparrow$$

$$\sum M_c = 0 = \left(\frac{1}{2}\right)(3')\left(\frac{9}{EI}\right)\left(9 + \frac{2}{3} \cdot 3\right) + \frac{1}{2}(6')\left(\frac{-18}{EI}\right)\left(3 + \frac{1}{3} \cdot 6\right)$$

$$+ \frac{1}{2}(3')\left(\frac{-18}{EI}\right)\left(\frac{2}{3} \cdot 3\right) + M_c = 0 \rightarrow M_c = \frac{175.5}{EI} \curvearrowright$$



$$\frac{1}{2}(3)\left(\frac{9}{EI}\right) = \frac{13.5}{EI}$$

$$\frac{13.5}{EI} - \frac{1}{2}(6)\left(\frac{18}{EI}\right) = \frac{-40.5}{EI}$$

$$-\frac{40.5}{EI} - \frac{1}{2}(3)\left(\frac{18}{EI}\right) = \frac{-67.5}{EI}$$

$$\frac{2}{3}(3)\left(\frac{13.5}{EI}\right) = \frac{27}{EI}$$

$$\frac{27}{EI} + \frac{2}{3}(3)\left(\frac{13.5}{EI}\right) = \frac{54}{EI}$$

V_{VC}
 θ_{VR}

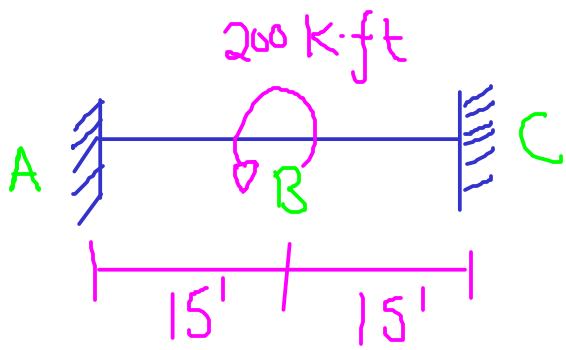
M_{VC}
 δ_{VR}

$$\theta_c = \frac{67.5}{EI}$$

$$\delta_c = \frac{-175.5}{EI}$$

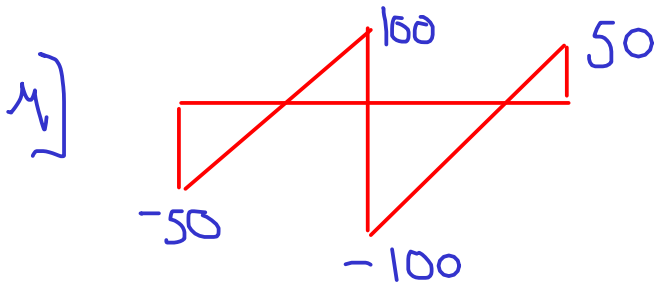
$$\delta_{MAX A-B} = \frac{54}{EI}$$

$$-\frac{175.5}{EI}$$

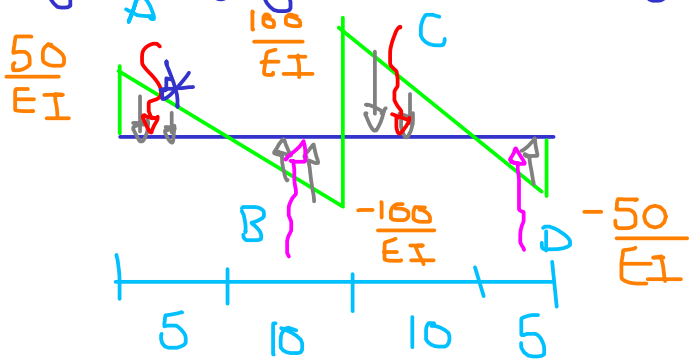


¿ $\delta_{\text{vert. máx.}}$?

¿ $\theta_{\text{máx.}}$ & ubicación?



Viga Conjugada (sin apoyos)



Equilibrio por las cargas

$$A = \frac{1}{2} (5') \left(\frac{50}{EI} \right) = \frac{150}{EI}$$

$$B = \frac{1}{2} (10') \left(\frac{100}{EI} \right) = \frac{500}{EI}$$

$$C = \frac{1}{2} (10') \left(\frac{100}{EI} \right) = \frac{500}{EI}$$

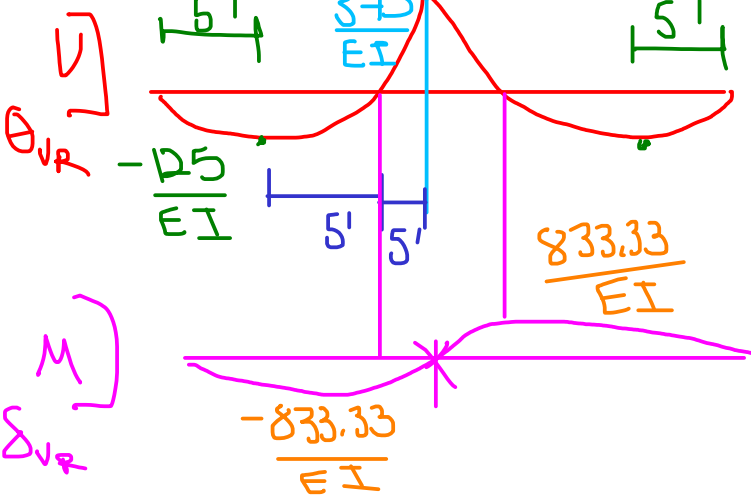
$$D = \frac{1}{2} (5') \left(\frac{50}{EI} \right) = \frac{150}{EI}$$

$$* E_c = y = mx + b$$

$$y = \frac{-100 - 50}{15} x + 50 = -10x + 50$$

$$-10x + 50 = 0$$

$$\hookrightarrow x = 5 \text{ ft.}$$



$$\frac{1}{2} \left(\frac{50}{EI} \right) (5) = \frac{125}{EI}$$

$$\frac{1}{2} \left(\frac{100}{EI} \right) (10) = \frac{500}{EI}$$

$$\frac{500}{EI} - \frac{125}{EI} = \frac{375}{EI}$$

$$\frac{2}{3} (10') \left(\frac{125}{EI} \right) = \frac{833.33}{EI}$$

$$\theta_{\text{MÁX}} = \frac{375}{EI} @ \ell$$

$$\delta_{\text{MÁX}} = \frac{833.33}{EI}$$

2 10 ft de cada apoyo.